



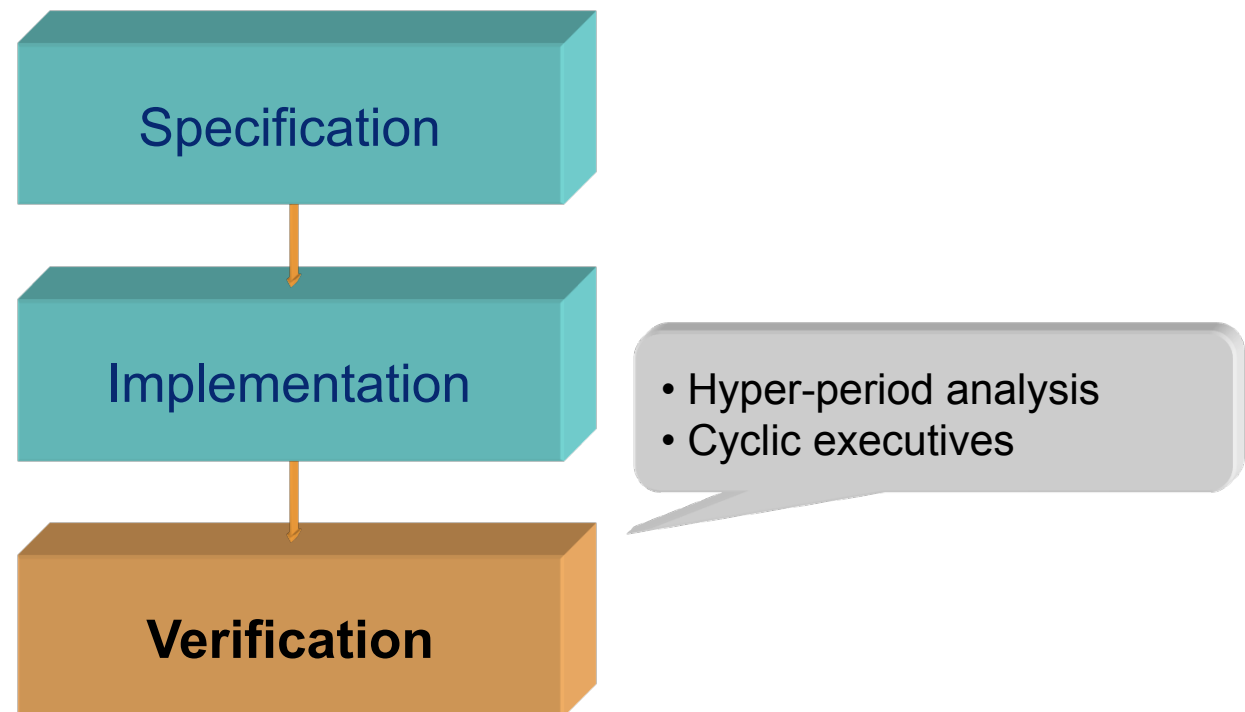
# Real-Time Systems

## Lecture #10

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# Real-Time Systems



# Feasibility tests

## What types of feasibility tests exist?

- Hyper period analysis (for any type of scheduler)
  - In an existing schedule no task execution may miss its deadline
- Processor utilization analysis (static/dynamic priority scheduling)
  - The fraction of processor time that is used for executing the task set must not exceed a given bound
- Response time analysis (static priority scheduling)
  - The worst-case response time for each task must not exceed the deadline of the task
- Processor demand analysis (dynamic priority scheduling)
  - The accumulated computation demand for the task set under a given time interval must not exceed the length of the interval

# Hyper period analysis

## Motivation:

- When it is not obvious which feasibility analysis should be used for a given task set and a given scheduler it is always possible to generate a schedule by simulating the execution of the tasks, and then check feasibility for individual tasks.
- The schedule interval that is sufficient to investigate is related to the hyper period of the task set, that is, the least common multiple (LCM) of the task periods.

NOTE: Unless the periods of all tasks are harmonically related (multiples of each other) hyper-period analysis will in general have an exponential time complexity.

# Hyper period analysis

## Schedule interval to investigate:

- For synchronous task sets:  $\forall i, j : O_i = O_j$   
It is sufficient to investigate the interval  $[0, P]$   
where  $P$  is the hyper period of the task set.
- For asynchronous task sets:  $\exists i, j : i \neq j, O_i \neq O_j$   
It is sufficient to investigate the interval  $[0, P]$   
if no task instance that arrives within the interval  
executes beyond time  $P$ .  
  
In all other cases it is necessary to investigate  
more than one hyper period.

# Cyclic executives

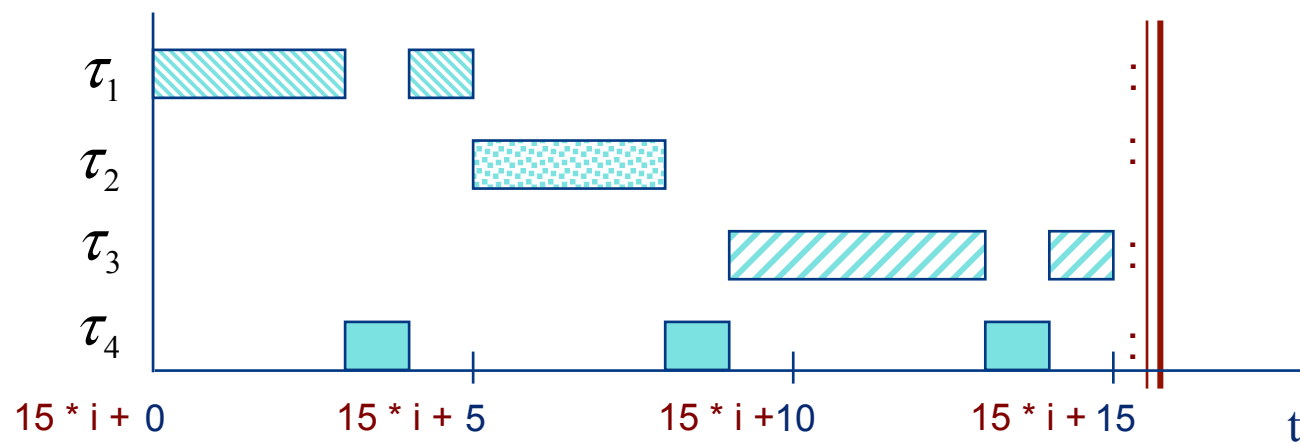
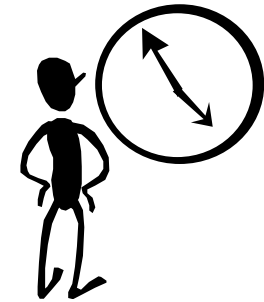


Because of its deterministic properties the cyclic executive is often the choice of scheduler in safety-critical real-time systems, such as automotive and aircraft applications.

# Cyclic executives

## General properties:

- Table-based schedule
- Feasibility test performed when generating table
- Schedule repeats itself (= “cyclic executive”)



# Cyclic executives

## General properties:

- Off-line schedule generation
  - Explicit start and finish times for each task are derived off-line, and chosen so that at most one task at a time requests access to the processor during run time.
- Mutual exclusion is handled explicitly
  - The schedule must be generated in such a way that a task switch is not made within a critical region (= no need for mutual exclusion support at run-time, e.g. mutex objects)
- Precedence constraints are handled explicitly
  - The schedule must be generated in such a way that specified task execution orderings are respected (= no need for task synchronization at run-time, e.g. semaphores)



# Cyclic executives

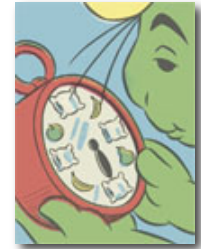
## Advantages:

- Communication between tasks is facilitated
  - The time instant when data becomes available is known
  - Task execution can easily be adapted to any existing time-slot network protocol (e.g., TTCAN, FlexRay).
- Low overhead for scheduling decisions
  - Everything is pre-planned, time table guides the run-time system
  - Feasibility test is done off-line during time table generation
- Task execution becomes very deterministic
  - Simplifies feasibility tests (compare finish time against deadline)
  - Simplifies software debugging (increased observability)
  - Simplifies fault tolerance (natural points in time for self control)

# Cyclic executives

## Disadvantages:

- Low flexibility (a.k.a. the "Skalman" factor)
  - The run-time system cannot adapt its schedule to changes in the task set or in the system environment
- External events are not handled efficiently
  - Data from I/O-based events (interrupts) may not be consumed directly by a periodic task due to the pre-planned schedule, which could lead to long response times.
  - An external event with a short deadline must be handled by a task with short period, which may lead to resource waste
- Not so efficient for tasks with "bad" periods
  - Tasks with mutually inappropriate periods give rise to large time tables, which may require more program code and/or data



# Cyclic executives

## How is the schedule generated?

- Simulation of pseudo-parallel execution:
  - Simulate a run-time system with a (myopic) priority-based scheduler and then "execute" the tasks on that simulator.
  - Example: find a schedule by simulating a run-time system with the (dynamic priority) earliest-deadline-first scheduler.
- Exhaustive search:
  - Use an algorithm that searches for a feasible schedule by considering all possible execution orders for the tasks.
  - Example: use the well-known A\* search algorithm to find a feasible (optimal or non-optimal) schedule.

If the simulated scheduler or search algorithm is optimal for the given system model a feasible schedule will be found whenever one exists.

# Cyclic executives

## How is the size of the time table restricted?

- Only cyclic schedules are considered:
  - Schedule is repeated with a cycle time (“**hyper period**”) that is equal to the LCM (“**least common multiple**”) of the task periods.
  - Tasks that are not periodic, or that have very long periods, can be handled by reserving time slots in the schedule for a “server” that can handle such special tasks when they arrive.
- Suitable task periods are chosen:
  - To obtain reasonably long cycle times, the task periods should (if application allows) be adjusted to be multiples of each other.
  - Example:
    - periods 7, 13, 23 ms  $\Rightarrow$  cycle time 2093 ms, but
    - periods 5, 10, 20 ms  $\Rightarrow$  cycle time 20 ms

# Cyclic executives

## How is the scheduler implemented?

- Use a circular queue that corresponds to the time table
  - Each element in the queue contains start and finish times for a certain task (or task segment in case of preemptive scheduling)
  - The elements in the queue are sorted by the start time
- Use clock interrupts
  - When a task starts executing, a real-time clock is programmed to generate an interrupt at the start time of the next (the one whose start time is closest in time) element in the queue.
  - When the interrupt occurs, the next element in the circular queue is fetched and the procedure is repeated.

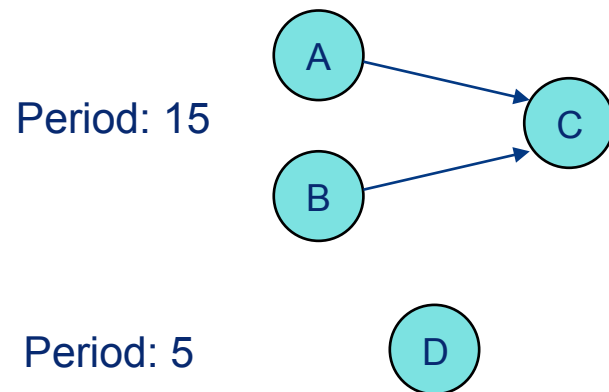
# Cyclic executives

## Remarks:

- Emulating a cyclic executive
  - By assigning offsets to tasks in a priority-based run-time system it is possible to mimic the behavior of a cyclic executive.
  - Example: assigning offsets to AFTER() operations in TinyTimber
- Emulating other priority-based schedulers
  - By generating a table-based schedule by simulation it possible to mimic the behavior of tasks with static priorities on a run-time system with dynamic priorities (and vice versa).
  - Example: simulating the rate-monotonic (static priority) scheduler to generate a time table that is used to emulate a cyclic executive on the (dynamic priority) TinyTimber run-time system.

# Example: simulating EDF

**Problem:** Assume a system with tasks and precedence constraints according to the figure below. Timing constraints for the tasks are given in the table. Generate a cyclic schedule for these tasks by simulating preemptive earliest-deadline-first (EDF) scheduling.



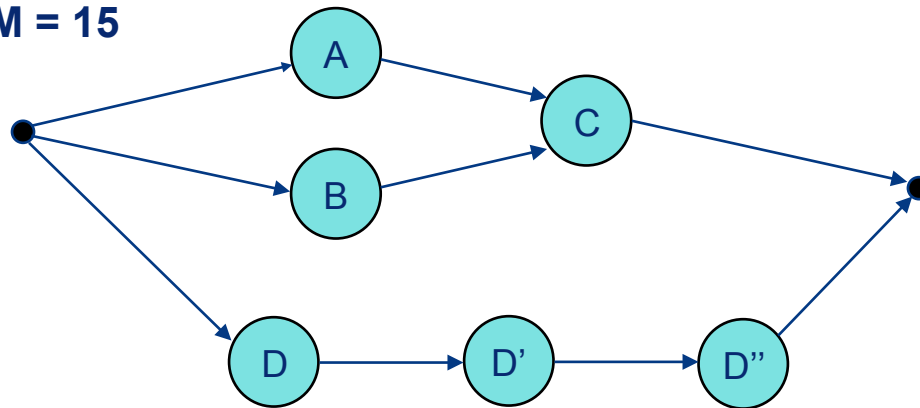
Task	$C_i$	$O_i$	$D_i$	$T_i$
A	4	0	7	15
B	3	0	12	15
C	5	0	15	15
D	1	3	1	5

# Example: simulating EDF

Begin by calculating the LCM of the tasks:  $\text{LCM}\{15,5\}=15$

Then generate a new version of the task graph with cycle time 15.

LCM = 15



Task	$C_i$	$O_i$	$D_i$	$T_i$
A	4	0	7	15
B	3	0	12	15
C	5	0	15	15
D	1	3	1	15
D'	1	8	1	15
D''	1	13	1	15

Observe that D must execute  $15/5 = 3$  times within the cycle, hence instances D' and D'' in the new graph.



## Example: simulating EDF

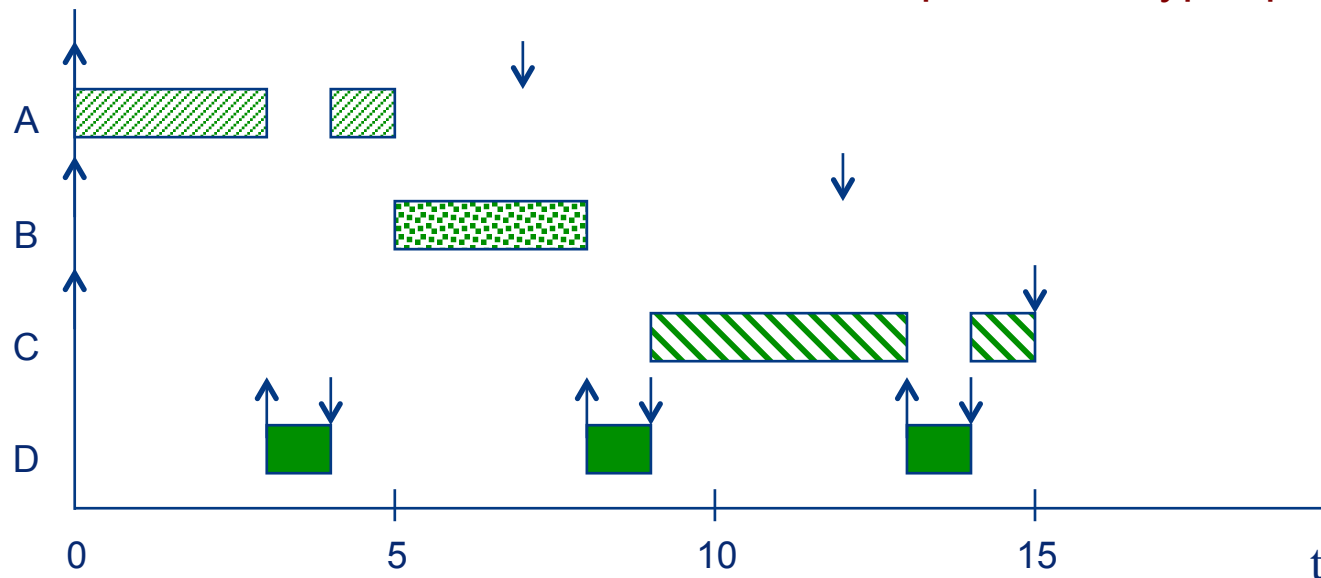
Now generate a schedule by assuming preemptive, earliest-deadline-first scheduling and simulate execution of the tasks:

1. A is scheduled first since it has the earliest deadline among the tasks (A and B) that are ready at  $t = 0$ .
2. D becomes ready at  $t = 3$  and preempts A since D's deadline is closer in time than A's and B's deadlines.
3. A resumes its execution at  $t = 4$  and finishes at  $t = 5$ .
4. B is scheduled at  $t = 5$  and finishes at  $t = 8$ . C becomes ready.
5. D' becomes ready and is scheduled at  $t = 8$  since the deadline of D' is closer in time than C's deadline.
6. C is scheduled at  $t = 9$ .
7. D'' becomes ready at  $t = 13$  and preempts C since the deadline of D'' is closer in time than C's deadline.
8. C resumes its execution at  $t = 14$  and finishes at  $t = 15$ .

# Example: simulating EDF

Static schedule:

NOTE: Since no task executes beyond  $t = 15$ , it is sufficient to generate, and check feasibility of, a schedule that spans one hyper period  $[0, 15]$



Cyclic time table:

(A,0,3) (D,3,4) (A,4,5) (B,5,8) (D',8,9) (C,9,13) (D'',13,14) (C,14,15)