

Exercise session
(Memory management / Virtual Memory)

Operating Systems – EDA092/DIT400

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Exercise 1

Jake and Finn have a computer whose memory access time is 150 nanoseconds and whose page-fault service time is 5 milliseconds. A process previously run in an operating system without virtual memory was 2 times faster than the same process run by the actualized operating system (the latter having virtual memory). Every how many page accesses are Jake and Finn experiencing a page fault on average? Would buying a new disk able to bring the page-fault service time to 2 milliseconds make the process no more than 1.5 times slower in the new operating system (compared to the previous one)?

Exercise 1 - solution

$$\begin{aligned} \text{EAT} &= (1 - p) \times (150 \text{ nanoseconds}) + p (5 \text{ milliseconds}) \\ &= (150 - p \times 150 + p \times 5,000,000) \\ &= 150 + p \times 4,999,850 \end{aligned}$$

Question 1

Without virtual memory $p = 0 \rightarrow \text{EAT} = 150$

With virtual memory $150 + p \times 4,999,850 = 2 \times 150$

$$p = 0.00003$$

1 page fault every $1/p$ (33333) on average

Question 2

$$150 + 0.00005 \times 1,999,850 < 1.5 \times 150 ?$$

$$250 < 225? \rightarrow \text{NO}$$

Exercise 2

- Given the following reference string

7 2 1 2 0 1 1 4 2 3 0 7 0 1 2 7 7 3 0 0 3 0 3

and assuming 4 frames are available, find:

- The minimum number of page faults we can observe
- The extra page faults caused by the FIFO replacement algorithm
- The extra page faults caused by the LRU replacement algorithm

Exercise 2 - solution

OPTIMAL

7 2 1 2 0 1 1 4 2 3 0 7 0 1 2 7 7 3 0 0 3 0 3

7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	0	0	0	0	0
	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
		1	1	1	1	1	4	4	3	3	3	3	3	3	3	3	3	3	3	3	3
				0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1

Page faults

1	1	1	0	1	0	0	1	0	1	0	0	0	1	0	0	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Exercise 2 - solution

FIFO

7 2 1 2 0 1 1 4 2 3 0 7 0 1 2 7 7 3 0 0 3 0 3

7	7	7	7	7	7	7	7	4	4	4	4	4	4	4	2	2	2	2	2	2	2	2
	2	2	2	2	2	2	2	2	2	3	3	3	3	3	3	3	3	3	3	3	3	3
		1	1	1	1	1	1	1	1	1	1	7	7	7	7	7	7	7	0	0	0	0
				0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1

Page faults

1	1	1	0	1	0	0	1	0	1	0	1	0	1	1	0	0	1	1	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Exercise 2 - solution

LRU

7 2 1 2 0 1 1 4 2 3 0 7 0 1 2 7 7 3 0 0 3 0 3

7	7	7	7	7	7	7	4	4	4	4	7	7	7	7	7	7	7	7	7	7	7	7
	2	2	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	0	0	0	0	0
		1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	3	3	3	3	3	3
				0	0	0	0	0	3	3	3	3	3	2	2	2	2	2	2	2	2	2

Page faults

1	1	1	0	1	0	0	1	0	1	1	1	0	1	1	0	0	1	1	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Exercise 2 - solution

- Minimum is 8
- FIFO is +3
- LRU is +4

Exercise 3

- Given processes P_1, P_2, P_3 and P_4 having sizes of 20, 25, 50 and 4 pages and given a total number of frames equal to 80 (10% of which reserved to the OS), compute the number of frames allocated to each process if frames are allocated proportionally to the size of each program

Exercise 3 - solution

- Frames for P_1 : $20/99 * 72 = 14$
- Frames for P_2 : $25/99 * 72 = 18$
- Frames for P_3 : $50/99 * 72 = 36$
- Frames for P_4 : $4/99 * 72 = 2$

Notice that I'm rounding down instead of up otherwise I will violate the assumption that 8 pages should be devoted to the OS!

Exercise 4

- Suppose a process P has size of 100 bytes. Compute (1) the number of wasted bytes caused by internal fragmentation if the page and frame sizes are set to 2^4 bytes and (2) the size in bits of the page table (assume each frame entry requires 1 byte and that dirty bits are also used to speed the swap out of pages).

Exercise 4 - solution

- Page size = 16 bytes
- Number of pages required = $\text{ceil}(100/16) = 7$
- Wasted bytes because of internal fragmentation $16 - 100\%16 = 12$ bytes
- Page table = $7 * (8 + 1 + 1) = 70$ bits
 - 8 bits \rightarrow frame entry
 - 1 bit \rightarrow valid/invalid bit
 - 1 bit \rightarrow dirty bit